

### Tensor products of locally $m$ -convex $H^*$ -algebras. Structure theory

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#### ABSTRACT

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In 1964, L. Grove [2] considered tensor products of  $H^*$ -algebras of W. Ambrose [1]. In this work we consider tensor products of locally  $m$ -convex  $H^*$ -algebras [3]. In particular, we prove that the tensor product of two Hausdorff locally  $m$ -convex  $H^*$ -algebras, in the projective tensor product topology, is an algebra of the same type. The existence of a canonical basis in a tensor product algebra, as before, is crucial for its structure. So, we examine conditions under which, there is such a basis. Based on this, we succeed among other things, a decomposition of the algebra in question, through minimal closed 2-sided ideals, getting thus the analogous here second Wedderburn structure theorem.

#### References

- [1] W. Ambrose, *Structure theorems for a special class of Banach algebras*, Trans. Amer. Math. Soc. 57 (1945) 364–386.
  - [2] L.C. Grove, *Tensor products of  $H^*$ -algebras*, Thesis, University of Minnesota, 1964.
  - [3] M. Haralampidou, *On locally convex  $H^*$ -algebras*, Math. Japonica 38 (1993) 451–460.
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